Running head: Predator-mediated Allee effects

Title: Predator-mediated Allee effects in multi-prey systems

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Abstract

Allee effects can have significant consequences for small populations and understanding the causal mechanisms for such effects are important for guiding conservation actions. One proposed mechanism is through predation where a type II functional response leads to increasing predation rates as prey numbers decline. However, models to support this mechanism have incorporated only a single declining prey in the functional response, which is likely an oversimplification. We re-evaluated the potential for predator-mediated Allee effects in a multi-prey system using Holling's disc equation. We also used empirical data on a large herbivore to examine how grouping behavior may influence the potential for predation-mediated Allee effects. Results based on a multi-prey expression of the functional response predict that Allee effects caused by predation on relatively rare secondary prey may not occur due to handling time of the abundant prey dominating the functional response to where secondary prey are largely “by-catch.” However, a predator-mediated Allee effect can occur if secondary prey live in groups and as the population declines, their average group size declines (a relationship seen in several species). In such a case, the rate that the number of groups declines is less than the rate the population declines. Thus the rate that a predator encounters a group remains relatively stable but when a predator kills one animal from smaller groups, the predation rate increases.

Key words: Allee effect, apparent competition, conservation, functional response, predator-prey interactions, Rangifer tarandus caribou, social organization
Introduction

Understanding mechanisms affecting small populations is critical for implementing effective conservation actions. Of particular importance for conservation are possible Allee effects (or inverse density dependence) that cause the per capita growth rate to decline as populations become smaller (Allee et al. 1949, Courchamp et al. 1999, Stephens et al. 1999). Allee effects greatly exacerbate extinction risk unless appropriate management is applied.

Documented mechanisms causing Allee effects include an insufficient number of conspecifics for efficient reproduction or predator avoidance (Courchamp et al. 1999, Stephens et al. 1999, Courchamp et al. 2008). Several studies have concluded that a predator-mediated Allee effect may be common when a predator displays a type II functional response in combination with, or in particular without, a numerical response to declines in the density of the rare prey species (Sinclair et al. 1998, Cantrell et al. 2001, Gascoigne and Lipcius 2004, Wittmer et al. 2005a, Angulo et al. 2007, Courchamp et al. 2008). The lack of a numerical response by the predator could arise where the rare prey species is declining, but because it is a minor component in the diet of the predator, the predator shows no change in number associated with its decline. It has been suggested that under such a scenario, the type II functional response alone is capable of creating an escalating mortality rate of prey as their numbers decline, thus causing an Allee effect (Sinclair et al. 1998, Gascoigne and Lipcius 2004).

In their recent book entitled “Allee effects in ecology and conservation,” Courchamp et al. (2008) point out “although single species models have been
very useful for understanding Allee effects, their failure to account for interspecific relationships is in many cases an oversimplification." We agree that this is the case when considering predator-mediated Allee effects. Although the implications of various combinations of functional and numerical responses have been discussed in detail (e.g., Holling 1959a, Oaten and Murdoch 1975, Messier 1995), these investigations were based on single prey systems or at least were focused on the dominant prey species in the system. However, the potential for an Allee effect is only relevant to prey that are a small component of the total biomass available to the predator in the multi-prey system. Otherwise, the predator would likely show a conventional numerical response, negating the potential for an Allee effect.

Our objectives are twofold. First, we re-evaluate predictions involving predator-mediated Allee effects (Messier 1995, Sinclair et al. 1998, Gascoigne and Lipcius 2004) by including multiple prey species in the functional response. We are interested in the situation where predators forage on declining rare prey (i.e., secondary prey) but spend the majority of their time eating more abundant primary prey (Bergerud and Elliot 1986, Seip 1992, Robinson et al. 2002, Wittmer et al. 2005a). Others have recognized that the relationship between predators and prey not only depends on their abundance, but also the social organization of the various species involved (e.g., Hamilton 1971, Fryxell et al. 2007). Therefore, our second objective was to examine how group size changes with population density and how this, in turn, affects predation rates under scenarios of declining secondary prey. We use data from the endangered mountain
ecotype of woodland caribou (*Rangifer tarandus caribou*) that are declining in numbers over most of their distribution (Wittmer et al. 2005b).

Methods

Functional response model

If prey did not live in groups and were part of a single predator, single prey system, the type II functional response of that predator would follow the “disc equation” of Holling (1959b):

\[ y_t = \frac{aNT}{1 + aNT_h} \quad \text{eqn. 1} \]

where \( y_t \) is the total number of prey killed per predator over a total period of time \( T \), and \( a \) is the searching rate of the predator, \( N \) is the prey density, and \( T_h \) is the handling time that includes chasing, killing, consuming and digesting one prey.

The mortality rate of the prey caused by predation (i.e., predation rate) can then be determined from the number of prey killed divided by the prey population size (Messier 1994). The number of prey killed is referred to as the “total response,” and is simply the product of the functional and numerical response (Holling 1959a, Messier 1994).

If there are more than one prey species (in the following example we use 2 prey species) and for simplicity, all prey species have the same handling time, \( N \) becomes the sum of the number of each species (*sensu* Abrams 1990) and:

\[ y_t = \frac{a(N_1 + N_2)T}{1 + a(N_1 + N_2)T_h} \quad \text{eqn. 2} \]
where $y_t$ is now the total number of both prey species killed per predator. If, for this simple model, we assume that the predator encounters prey in proportion to their abundance and, once encountered, the probability of killing is the same for each species, then we can divide $y_t$ into $y_1$ and $y_2$, that are the numbers of each prey species killed, based on their relative abundance.

Prey living in groups

If one of the species is found in groups, then $N_i$ is the number of groups, not individuals. What is critical in the group-size component of our model is that we assume the probability of a searching predator encountering a group is equal to encountering an individual (see Huggard 1993) and the predator kills only one group member at a time. These assumptions are unlikely true for all predator-prey systems, but are more likely to hold when the secondary prey are rare and exist in small groups (where Allee effects are expressed) and handling time is of sufficient duration to enable surviving members of the group to effectively escape (e.g., Huggard 1993, Hebblewhite and Pletscher 2002, Fryxell et al. 2007, Coleman 2008). For group sizes and thus number of groups ($N_i$) used in equation 2 to estimate predation rates at various population sizes, we first used the relationship between the average population size determined by Wittmer et al. (2005b) and observed groups sizes of mountain caribou in summer (see Field Data, below).

For all models, we use a handling time of 5 days per prey item and a search rate of 1 km$^2$ per day, $T$ is 30 days, and the prey density is individuals per
1,000 km². In the single prey models, we vary their numbers between 1 and 300. For the multi-prey models, we vary the numbers of secondary prey between 1 and 300 while keeping the primary prey stable at 1000. We first use a type 0 numerical response (i.e., no response) because we are interested in Allee effects of small populations. To enable further comparisons and because we varied the ratio of primary to secondary prey considerably in our models, we also incorporated a simple type I numerical response. The type I numerical response is based on 50 prey groups per predator (i.e., a linear response to prey density; e.g., Fuller 1989).

To investigate implications of animal group sizes beyond data available from caribou, we used equation 2 but varied the slope and shape of the relationship between group size and population size of the secondary prey, while keeping the number of primary prey stable at 1000 solitary animals. To maintain simplicity and because it was the suggested relationship for some species, we varied the slope (b) of the line (group size = 1 + bN₂) to have group sizes of 1, 2, 5 and 10 animals when there were 300 secondary prey but always 1 when the last animal remained.

**Field data**

Mountain caribou live in a multi-prey, multi-predator system in southeastern British Columbia, Canada, that includes up to 7 other ungulate species that are preyed on by up to 5 carnivore species (see Wittmer et al. 2005b for a detailed map of the study area and description of the physical environment). Mountain
caribou have been studied using radiotelemetry since 1984 and individuals from 18 populations have been monitored; however, 4 populations were so small and infrequently seen in summer that insufficient group size data were obtained and data from one population were not available for our analysis. Thus, data from 13 populations were available to determine the relationship between population size and group size.

Collared animals were located 2 to 4 times per month from a fixed-wing aircraft and the number of animals in the group was recorded whenever they were observed. Populations were censused from helicopters in March or early April when caribou are in open, high-elevation habitats and shortly after new snow fell (Wittmer et al. 2005b). The relationship between the average size of the population and mean group size was made for the summer season when caribou habitat overlaps with alternative prey and predators and that is when most predation occurs (Wittmer et al. 2005b).

To determine if the relationship between population size and group size is limited to mountain caribou and therefore not of broader utility, we also used data from moose (*Alces alces*; sampled within the central portion of the mountain caribou distribution) and elk (*Cervus elaphus*; sampled in neighbouring Banff National Park, Alberta, Canada). For both of these species, winter censuses from helicopter provided group sizes and population estimates that varied over time. We did not use moose and elk data for our modelling, but rather to determine if the group size relationship holds beyond caribou.
Results

Modeling predation rates with prey living alone

In a single prey system, the type II functional response model shows an Allee effect if prey live alone and the predator has no numerical response (Fig. 1a, prey alone). When we added a type I numerical response to the type II functional response the Allee effect disappears (Fig. 1b, prey alone); that is, the predation rate declines as the population declines because there are fewer predators. In a multi-prey system with primary prey that are stable and abundant (1000), and a rarer (0-300), declining secondary prey and no predator numerical response to either prey, the Allee effect on the secondary prey is weaker than in the single prey scenario (Fig. 1a vs. 1c, prey alone). Predation rate actually changes very little as the rare prey declines. Because the magnitude of this Allee effect is proportional to the ratio of secondary prey to the sum of both secondary and primary prey, it would have been even less if primary prey were more abundant. If a type I numerical response is added (for both prey), the weak Allee effect on the secondary prey disappears (Fig. 1d, prey alone).

Prey living in groups: field data and models of predation rates with groups

To make model predictions with group living organisms, we first needed to determine how group size changes with population size and we used field data to obtain this empirical relationship. Between 1984 and 2006, 541 caribou were radio-collared and 2099 groups were seen during the summer season when the average group size was 3.8 individuals and 95% of groups had < 10 members.
Mean group sizes of mountain caribou were significantly larger in the larger populations, although the relationship was logarithmic (GLM Caribou: $R^2 = 0.64$, $F_{1, 11} = 19.15, p = 0.001$) (Fig. 2a). The largely solitary moose show a similar trend (bootstrapped 95% CIs do not overlap) (Fig. 2b). The magnitude of change was strongest for elk (Figs. 2c-d; GLM Eastern Banff: $R^2 = 0.79$, $F_{1, 22} = 80.42$, $p = 0.001$, $b=$; GLM Western Banff: $R^2 = 0.59$, $F_{1, 22} = 31.35$, $p = 0.001$). Moose and elk were not used in model scenarios, but simply to ensure the relationship is not limited to caribou.

In all cases, the group living scenario resulted in lower predation rates (Fig. 1). With a single group-living prey and no numerical response, there was an Allee effect that became most pronounced at < 50 animals (Fig. 1a, groups). When we add the numerical response, the Allee effect again disappears (Fig. 1b, groups). In the multi-species scenario however, the Allee effect exists regardless of whether the predator does or does not show a numerical response (Fig. 1c-d, groups). The strength of the Allee effect increases the more the group size declines with declining population size (Fig. 3).

**Discussion**

It is now common to find situations where declining, rare prey species are subject to elevated predation rates because predators are sustained by other primary prey (e.g., Seip 1992, Holt and Lawton 1994, Sweitzer et al. 1997, Sinclair et al. 1998, Norbury 2001, Robinson et al. 2002). In some instances, the declining prey appears to be subject to an Allee effect (Sinclair et al. 1998, Wittmer et al.)
Previous theoretical modeling of predator-mediated Allee effects considered only the rare, secondary prey species in the functional response of the predator. With a single prey species and no numerical response to the number of prey, our results, like those of Gascoigne and Lipcius (2004), predict a strong Allee effect. However, conditions for this scenario would be rare and may be limited to situations such as where exotic predators are preying on a species that has not evolved a predator avoidance strategy. Under this scenario, a predator may kill all individuals of the species quickly without switching to other prey species. It is likely more common, however, that the rare prey are but one of several prey species, and it is here that predictions of our functional response model differs from those of Messier (1995), Sinclair et al. (1998), and Gascoigne and Lipcius (2004).

**Multiple prey species in the functional response**

Given that the basis of the disc equation is the change in time a predator spends handling and searching for prey at different prey densities (Holling 1959b), all prey species should be included. Limiting the functional response to just the rare species that is suffering an Allee effect assumes that predators are spending enough time handling this species to affect predation rates to a significant degree. It also assumes that a change in the number of primary prey will not affect the number of the secondary species an individual predator will kill. This is clearly not true. If the number of primary prey greatly increases, then each predator will spend less time searching and more time handling primary prey than...
before. Conversely, if the number of primary prey declines, then each predator will spend more time searching and handling secondary prey than before. Combining all prey species into the disc equation causes the more common prey to dominate the functional response, or the amount of time a predator spends handling and searching for prey. This modification only required summing values of both prey species for the density and handling time expressed in Holling’s (1959b) disc equation.

When we modified the functional response to include an abundant but stable primary prey, our model predicted a very weak Allee effect when there is no numerical response and no Allee effect with a type I numerical response. In both cases, if there is an abundance of primary prey, the predation rate on the secondary prey is essentially density independent (i.e., “by catch”). In other words, changes in density of the secondary prey have little effect on the predation rate it experiences. This result differs from Messier (1995 Fig. 4b), Gascoigne and Lipcius (2004), and Sinclair et al. (1998) who used only one species in the functional response and a variety of ways to account for a numerical response. However, it is important to emphasize that “by catch” of secondary prey can still lead to extirpation by predators that are sustained by abundant primary prey (i.e., apparent competition; Holt and Lawton 1994) despite the absence of an Allee effect.
Prey living in groups with changing group size

All our models show that grouping behavior reduces predation rates, which is consistent with abundant theoretical and empirical work (e.g., Hamilton 1971, Clutton-Brock et al. 1999, Mooring et al. 2004, Fryxell et al. 2007). However, the mechanism we reveal is how an Allee effect could occur by including the effect of declining group size with declining population size. The underlying reason for this type of Allee effect is that the number of groups declines more slowly than the total population size. Thus the rate that groups are encountered may remain relatively stable but when one animal is killed from smaller groups, the predation rate increases. As a consequence, any individual in smaller groups is more likely to be killed by a predator encountering the group. This explanation likely accounts for some of the Allee effect observed in caribou in southeastern British Columbia (Wittmer et al. 2005a) where declining populations have resulted in smaller group sizes (the Allee effect is unlikely due to difficulty finding mates because pregnancy rates are high (92%) and invariant across all densities [Wittmer et al. 2005b]). Because a variety of species appear to be found in smaller groups when population sizes decline (e.g., Vincent et al. 1995, Borkowski 2000, McConville et al. 2009), this mechanism may be common but appears to have been overlooked in the Allee literature. For example, Courchamp et al. 2008 (p. 40) reported that caribou studied by Wittmer et al. (2005a) were prey “without gregarious behaviour”, even though Wittmer et al. (2005a) posit this mechanism: “because arboreal-lichen feeding woodland
caribou live in groups...the predation rate on smaller populations with smaller
groups would be higher.”

Although our models make several simplifying assumptions, this approach
was deliberate to make direct comparisons to previous work that made similar
assumptions (i.e., constant $a$ and $T_h$ across a range of prey density and simple,
instantaneous numerical response). We make the additional assumption that the
encounter rate for group living animals is the same as animals that live alone.
This is unlikely to be correct across a broad range of group sizes (Hebblewhite
and Pletscher 2002). But the magnitude of group size change in our system is
only 4.5 to 1, and in a forested ecosystem it is unlikely that this would have an
influence on encounter rates, particularly for a rare species. In support of this
approach, Fryxell et al. (2007) point out that “each doubling of prey density leads
to a much more modest increase in encounter frequency with groups.”

In summary, our models suggest that contrary to previous theory, Allee
effects on relatively rare declining prey are weak or non-existent in multi-prey
systems where functional responses of the predator are dominated by handling
primary prey. However, if prey live in groups and group size declines as prey
density declines, then this can contribute to an Allee effect. These results
highlight the need to evaluate risks associated with potential changes in group
size as populations decline. In addition, population augmentations could be used
as a tool to increase group sizes of resident populations of social ungulates to
levels that reduce the potential effect of predators (Mooring et al. 2004).
Alternatively, the level of predator management required to recover a group living
species may be different from species that live alone or if group size is not related to population size. However, more empirical studies are required to test our prediction of the relationship between rates of decline and group size in social animals including ungulates.

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References
McLellan et al. - Predator-mediated Allee effects


Figure captions

Figure 1. Predation rates of animals that live alone (- - -) or in groups (— — ) for: A) Single prey species (0-300) with a type II functional response, and no numerical response from the predator; B) Single prey species (0-300) with a type II functional response and a type I predator numerical response; C) Secondary prey species (0-300) with a type II functional response but when the predator’s primary prey population is stable (1000), and no numerical response from the predator; D) Secondary prey species (0-300) with a type II functional response and a type I numerical response but when the predator’s primary prey population is stable (1000).

Figure 2. Relationship between the size of populations and average group sizes: A) Mountain caribou population sizes and average group sizes observed in summer; B) Population size and average group size of Upper Columbia moose population (error bars are 95% CI, shown here because only 3 data points); C) Population size and average group size of Banff eastern elk population; D) Population size and average group size of Banff western elk population (adapted from Hebblewhite and Pletscher 2002).

Figure 3. The effect of various linear relationships between group size and population size (group size = $1 + bN_2$) on the predicted predation rate of a secondary prey species with a type II functional response but when the predator’s primary prey population is stable and maintained at 1000 animals.
Legend shows linear relationship varied from 1 animal per group at all population sizes (solitary species) to where group sizes increased to 2, 5, and 10 animals per group when there were 300 individuals in the population. In A, there is no numerical response. In B there is a type I predator numerical response to the number of groups.
Figure 1. McLellan et al.
Figure 2. McLellan et al.
Figure 3. McLellan et al.